

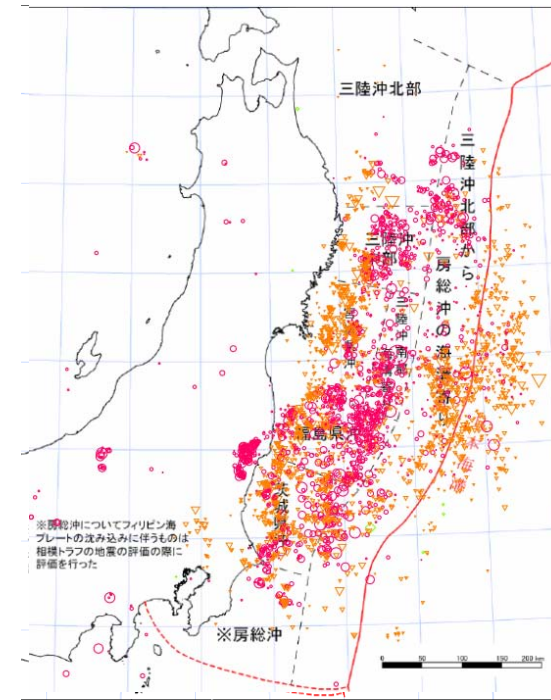
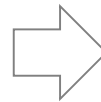
The M9 Tohoku–Oki Earthquake and Statistical Seismology

Yoshihiko Ogata, Institute of Statistical Mathematics

1. Long-term Probability forecasting and repeating earthquakes
2. Prediction and diagnostic analysis of seismic activity
3. Discrimination of foreshocks and their operational forecasting

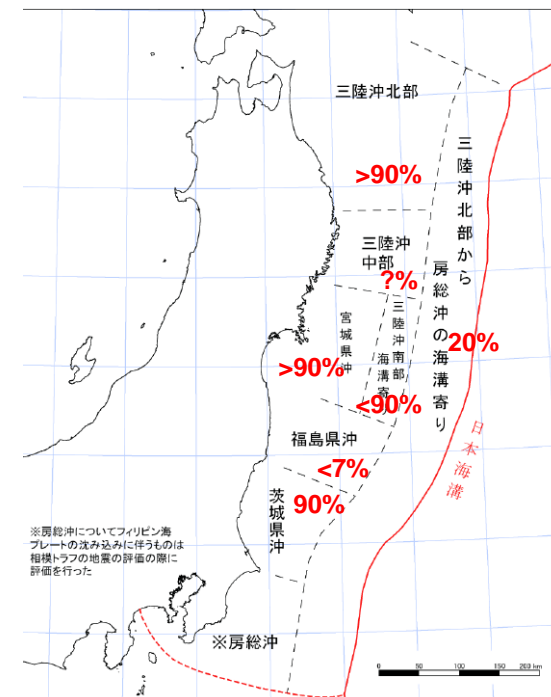
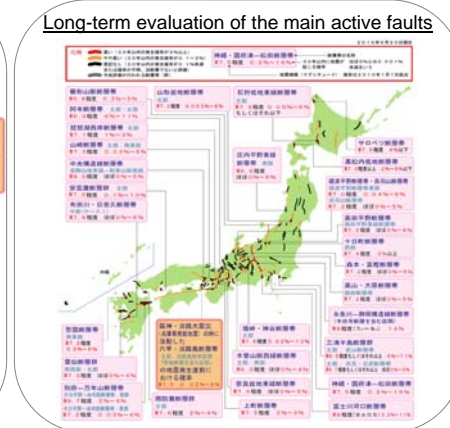


30
years
after

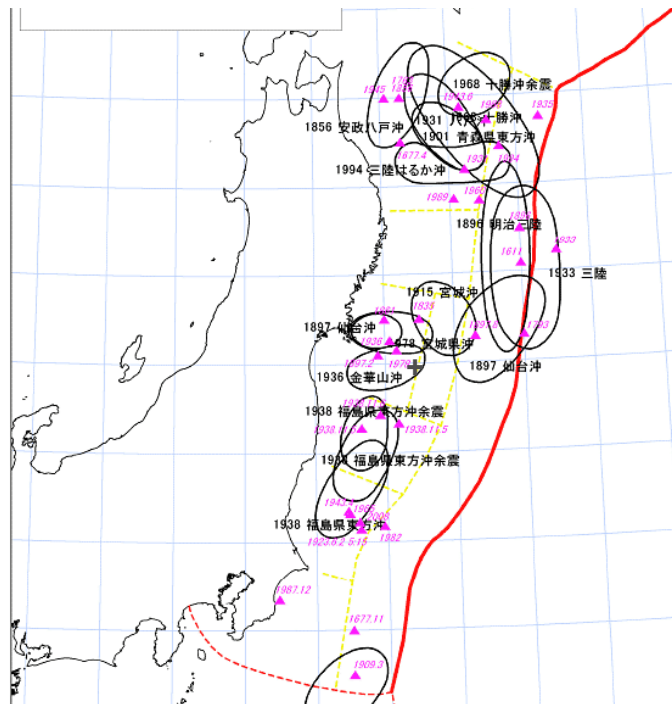


Long-term earthquake forecast

■ The Earthquake Research Committee (ERC) of Japan opens the probabilities that earthquakes will occur in the future at main active faults and subduction-zones in Japan to the public.

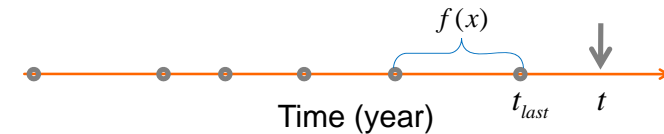


The main focal area of major Earthquakes From Sanriku-Oki to Boso-Oki (ERC, 1999)



Miyagi-Ken-Oki Earthquake

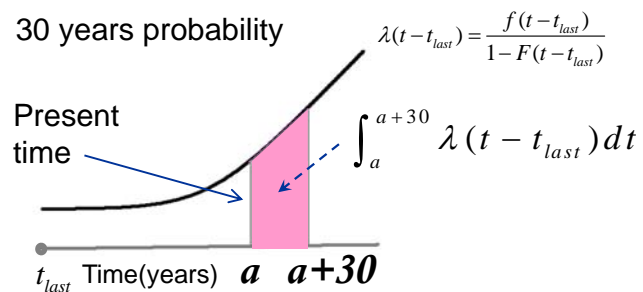
地震発生年月日	前回の地震からの経過年数(年)	地震の規模	備考
1793年2月17日		M8.2程度	連動の場合
1835年7月20日	42.4年	M7.3程度	単独の場合
1861年10月21日	26.3年	M7.4程度	単独の場合
1897年2月20日	35.3年	M7.4	単独の場合
1936年11月3日	39.7年	M7.4	単独の場合
1978年6月12日	41.6年	M7.4	単独の場合



Renewal process models

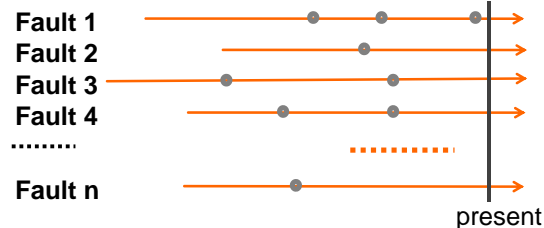
$$\lambda(t | History) = \lambda(t - t_{last}) = \frac{f(t - t_{last})}{1 - F(t - t_{last})}$$

30 years probability



30 years surviving probab. = $\exp(-\text{Area of } \text{shaded area})$

Active faults



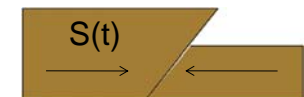
What is the BPT renewal process?

Probabilistic model for earthquake generation

Brownian relaxation oscillator process

$$S(t) = \lambda t + \sigma W(t)$$

Brownian motion with drift λ



S(t): Stress accumulation

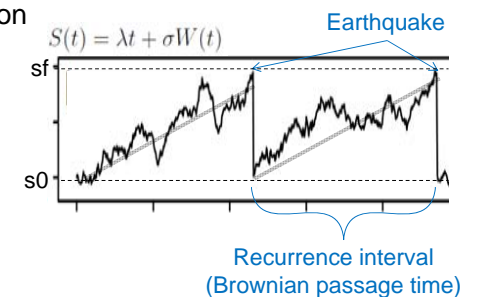
W(t): Standard Brownian motion

λ : Loading rate

σ : Perturbation rate

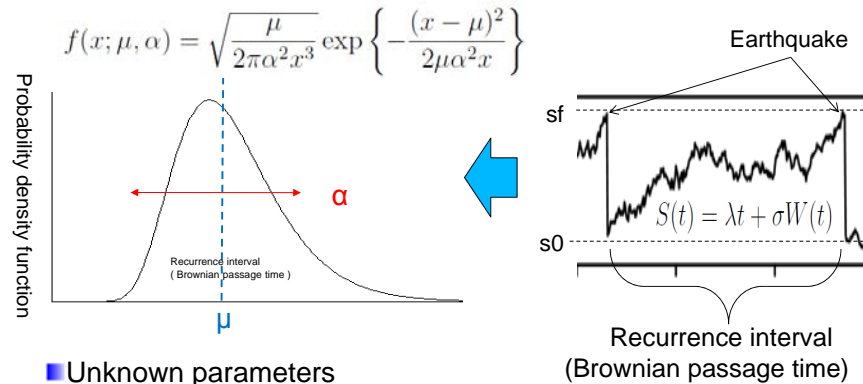
sf: Failure state

s0: Ground state



What is the BPT renewal process?

Brownian Passage Time (BPT) distribution



Unknown parameters

Mean $\mu = E[X_i] = \frac{s_f - s_0}{\lambda}$

Coefficient of variation $\alpha = \frac{\sqrt{\text{Var}[X_i]}}{E[X_i]} = \frac{\sigma}{\sqrt{\lambda(s_f - s_0)}}$

Forecasting method by ERC

Predictive distribution for interval time x from the latest earthquake to the next earthquake

Plug-in predictive density

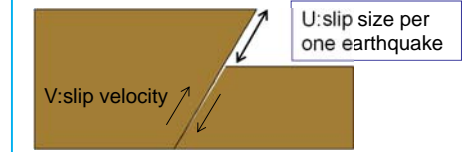
$$\hat{f}(x) = f(x|\hat{\mu}, \hat{\alpha})$$

$$\hat{\mu} = \begin{cases} \bar{X} = \sum_{i=1}^n X_i / n \\ T = U/V \end{cases} \text{ or}$$

$$\hat{\alpha} = 0.24$$

MLE from 4 active faults where a lot of earthquakes turned out.

Mean of past intervals
 $\mathbf{X} = (X_1 \cdots X_n)$



Proposal

S. Nomura (SOKENDAI D3)

Predictive distribution for interval time x from the latest earthquake to the next earthquake

Bayesian predictive density

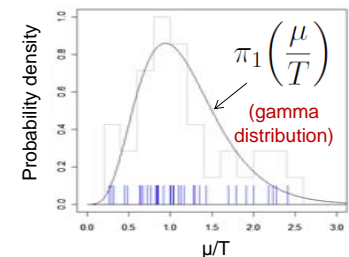
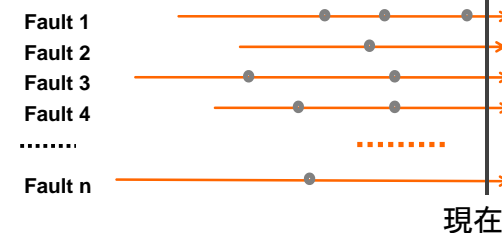
$$\tilde{f}(x) = \iint f(x|\mu, \alpha) \pi(\mu, \alpha|T, \mathbf{X}) d\mu d\alpha$$

$$\pi(\mu, \alpha|T, \mathbf{X}) \propto \underbrace{\pi(\mu, \alpha|T)}_{\text{prior density}} \times \underbrace{L(\mathbf{X}|\mu, \alpha)}_{\text{likelihood (BPT renewal process)}}$$

Merits of proposal method

- Its predictive performance will be more stable than plug-in methods.
- Both slip data $T=U/V$ and past intervals $\mathbf{X}=(X_1, \dots, X_n)$ are used.
- The estimation of α is not fixed and different among active faults.

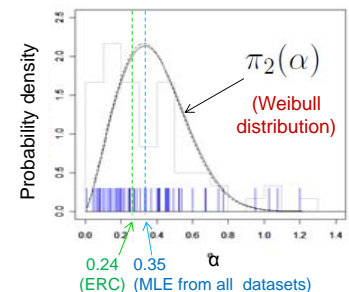
Estimation of prior distribution



ABIC and estimated prior distribution

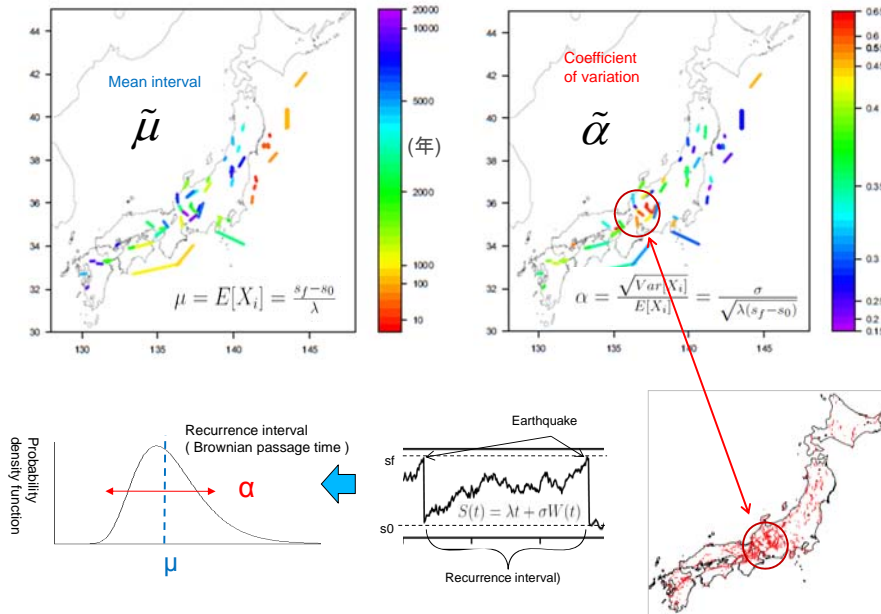
	$\pi_2(\alpha)$				
	Lognormal	Gamma	Weibull	Exp	Uniform
Lognormal	246.62	245.27	244.50	263.00	249.82
Gamma	245.78	244.44	243.67	262.66	249.94
Weibull	246.02	244.66	243.88	262.97	250.46
Exp	268.67	267.38	266.63	285.84	275.17
Uniform	251.86	250.48	249.69	268.92	257.63

$\pi_1\left(\frac{\mu}{T}\right)$



Maximum Posterior estimates

S. Nomura (SOKENDAI D3)

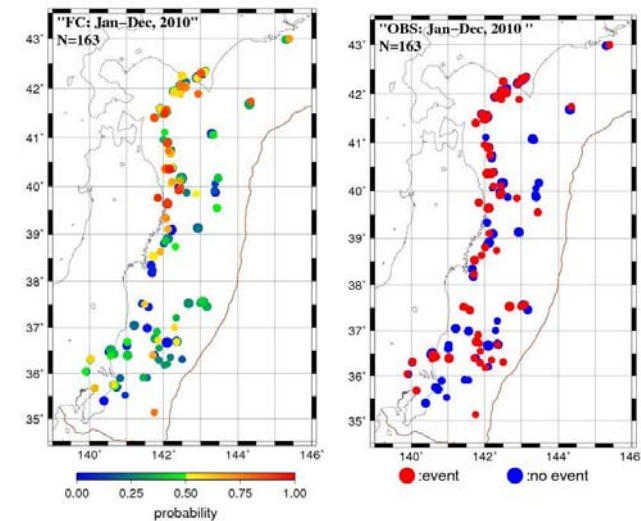


Okada, Uchida, Aoki (2011)

Renewal model (log Normal) for 163 repeating earthquake sequences
Estimation 1993 - 2009

Forecasted for 2010

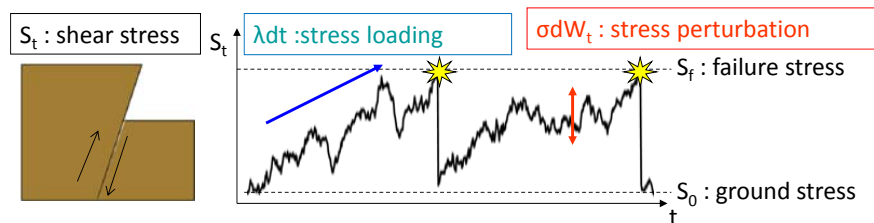
Result for 2010



Stochastic model for repeating earthquakes

Brownian relaxation oscillator process (e.g. Matthews et al. 2002)

$$dS_t = \lambda dt + \sigma dW_t \quad (W_t \text{ standard B.M.})$$



Interval lengths obey the BPT distribution:

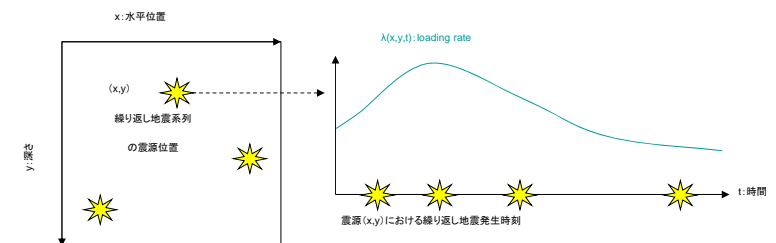
$$f(x|\mu, \alpha) = \sqrt{\frac{\mu}{2\pi\alpha^2 x^3}} \exp\left\{-\frac{(x-\mu)^2}{2\mu\alpha^2 x}\right\} \quad \begin{array}{l} \text{mean: } \mu = (s_f - s_0) / \lambda \\ \text{variance: } \alpha = \sigma / \sqrt{\lambda(s_f - s_0)} \end{array}$$

S. Nomura (SOKENDAI D3)

space-time model

- Non-stationary loading rates and dispersions

$$dS_t = \lambda(x, y, t) dt + \sigma(x, y, t) dW_t$$



- We cannot assume the BPT for the interval distribution.

Assume the following model

- $dS_t = \lambda_0 \lambda(x, y, t) dt + \sigma_0 \sqrt{\lambda(x, y, t)} dW_t$
 - λ_0 : Background loading rate
 - σ_0 : Background perturbation rate
 - $\lambda(x, y, t)$: space-time rates relative to the background loading rate λ_0

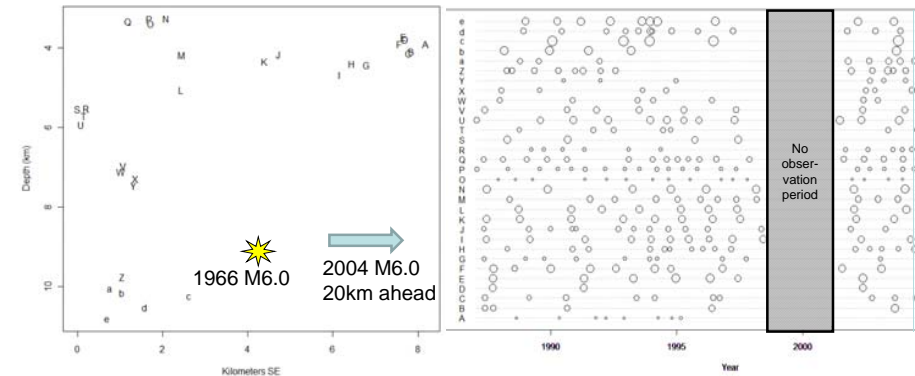
Then we have the BPT intervals for each (x, y) by time transformation $t' = \int \lambda(x, y, t) dt$

- $\lambda(x, y, t)$ is regarded as changes of stress loading velocity, and parameterized by a 3D spline function with smoothness constraints.
- Objective Bayesian procedure (ABIC) is applied to attain the optimal constraints.

Parkfield data (Nadeau)

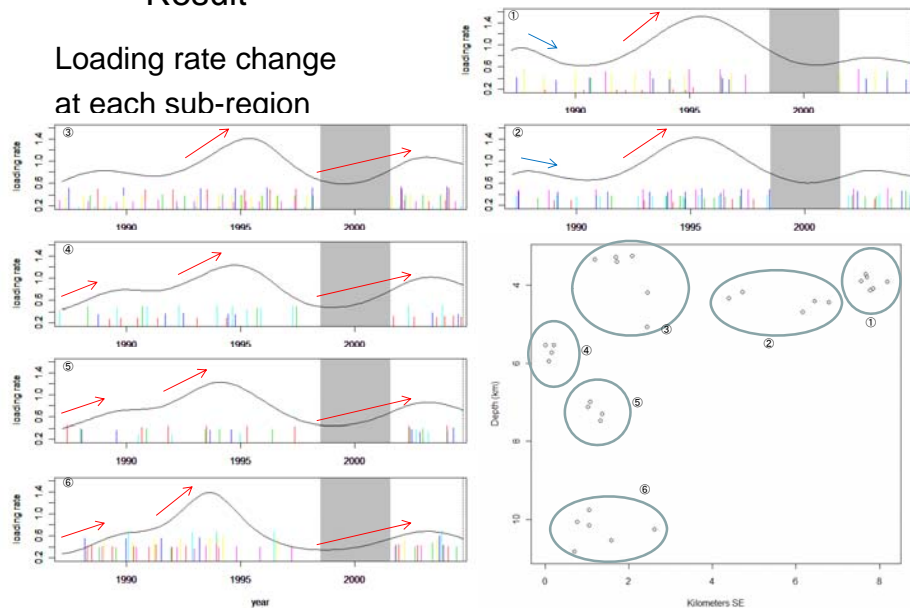
Micro-earthquakes (HRSN, Magnitude range $-0.5 \sim 2$)

- period 1987/1/1 \sim 2004/9/28 (preceding 2004 Parkfield) with missing data during 1998/7/1 \sim 2001/7/26



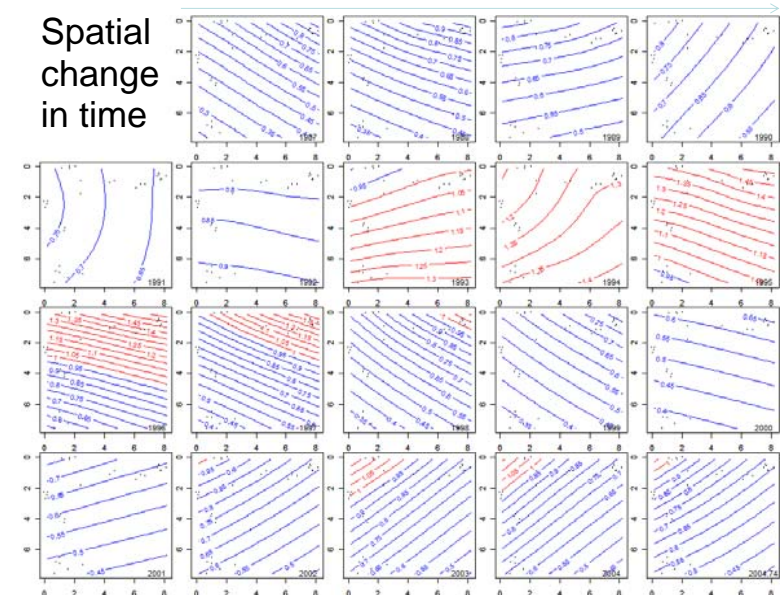
Result

Loading rate change at each sub-region



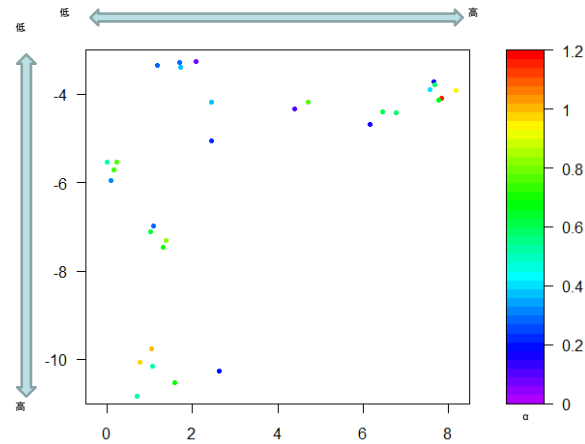
Result

Spatial change in time

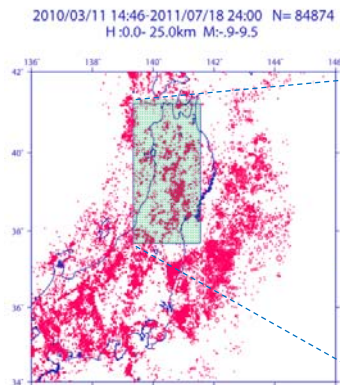


Result on the dispersion coeff. α

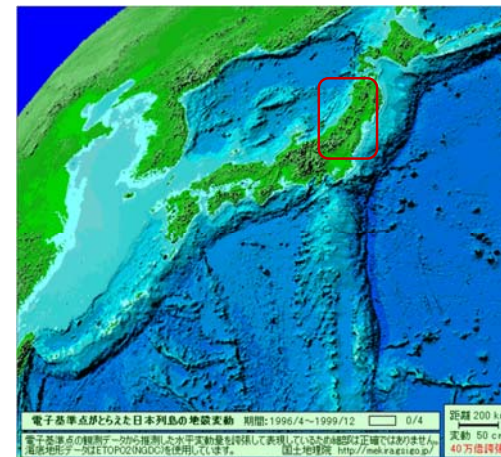
Dispersion coefficient α (proportional to the perturbation rate σ) is affected by the nearby earthquakes



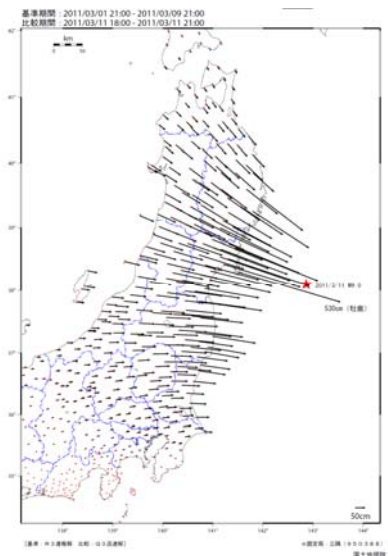
Prediction and diagnostic analysis of seismic activity

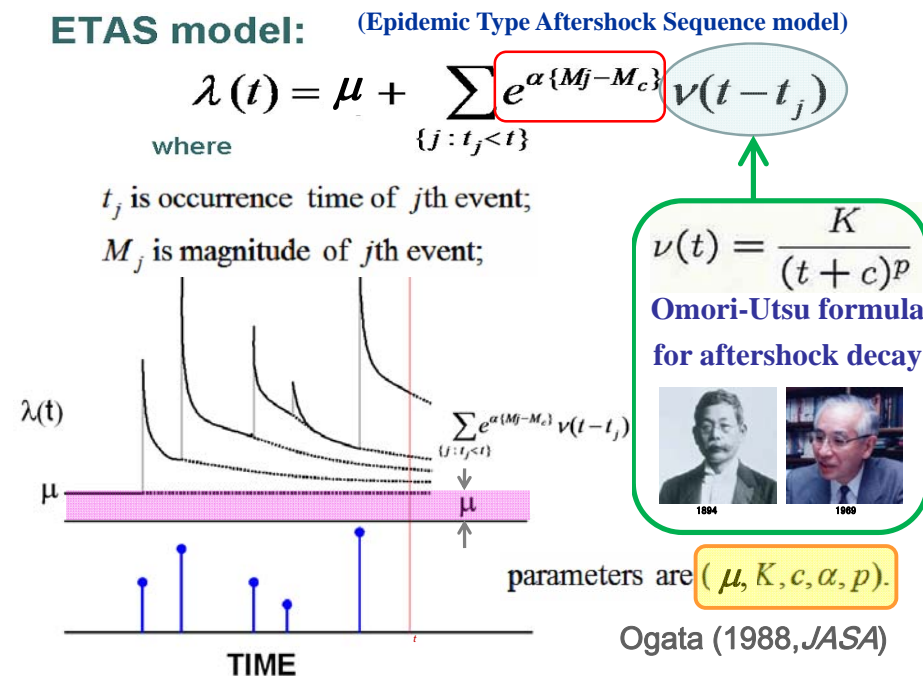
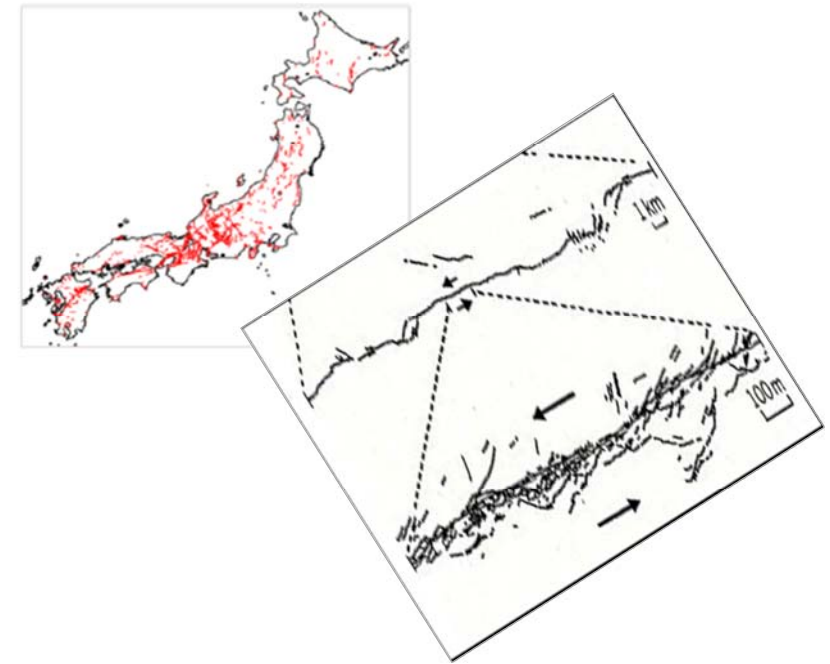
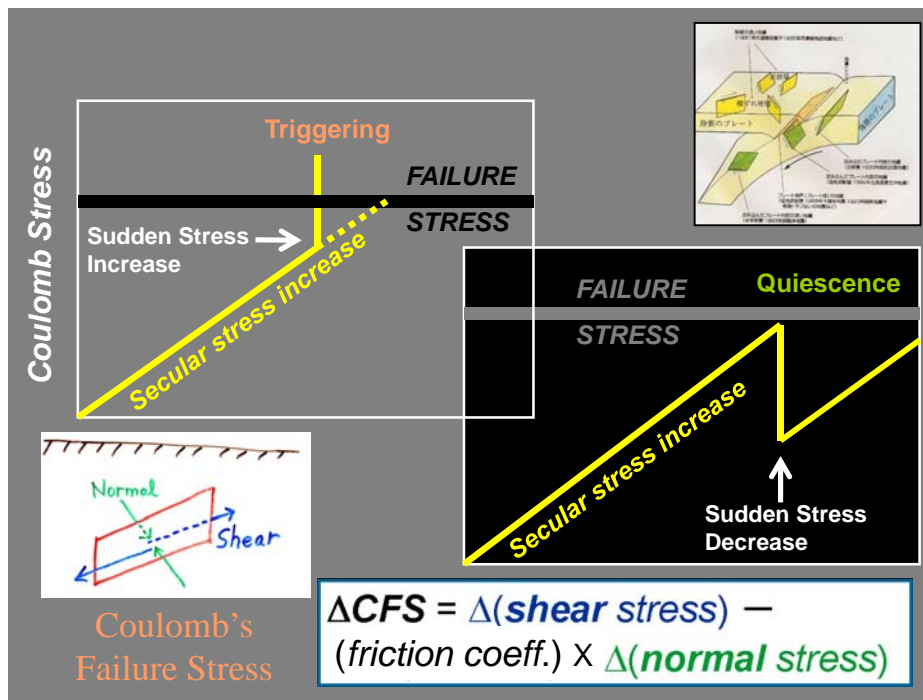


Geographical Survey Institute Deformation of Japanese islands



Coseismic dislocations of Tohoku-Oki earthquake of M9





Ogata (1988, J. Amer. Statist. Assoc.)



Observed time interval: $[S, T]$
Occurrence time data; t_1, t_2, \dots, t_n

Log-likelihood function:

$$\ln L(\theta; S, T) = \sum_{S < t_i < T} \ln \lambda_\theta(t_i) - \int_S^T \lambda_\theta(t) dt$$

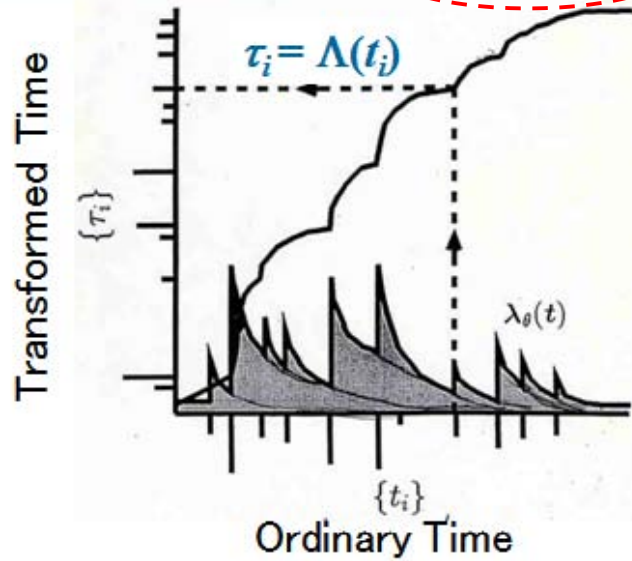
parameters are (μ, K, c, α, p) .

Maximize the function $\Rightarrow \hat{\theta} = (\hat{\mu}, \hat{K}, \hat{c}, \hat{\alpha}, \hat{p})$ **M.L.E.**

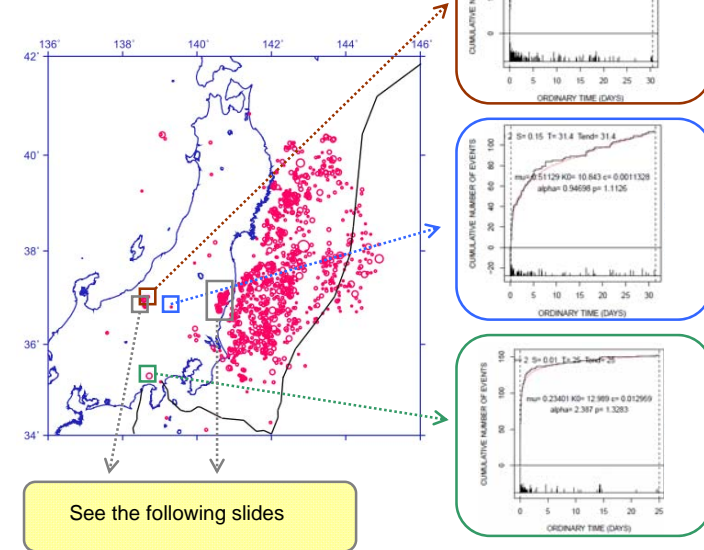
Computer codes available. Please visit WEB home page of our project team:
<http://www.ism.ac.jp/~ogata/Ssg/ssgE.html>

Theoretical cumulative number of the events:

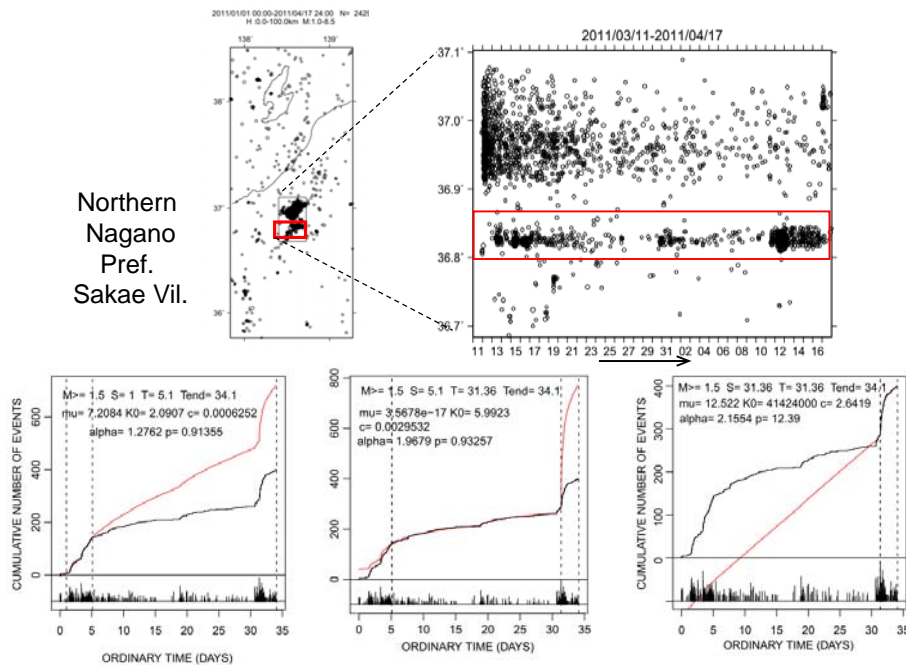
$$\Lambda(t) = \int_0^t \lambda(s) ds$$



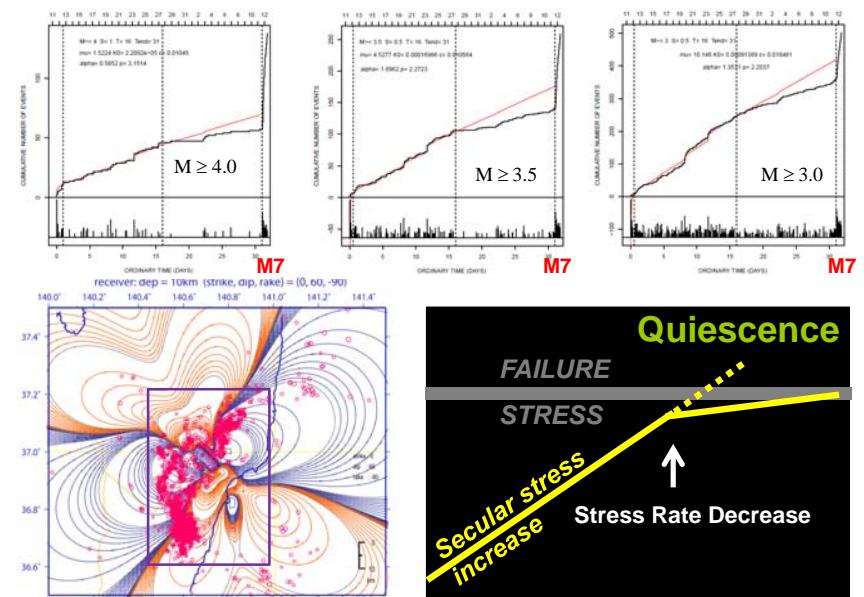
Triggered activities



Northern
Nagano
Pref.
Sakae Vil.



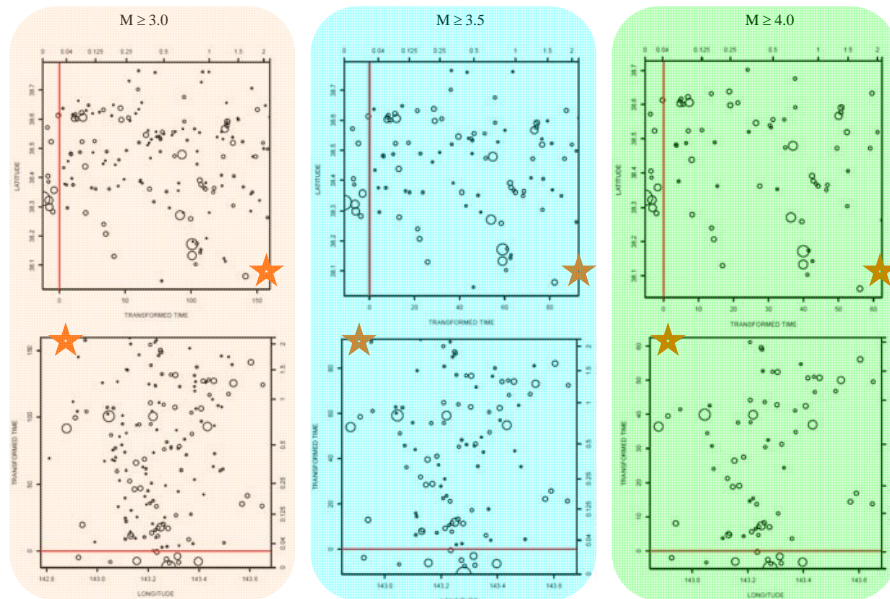
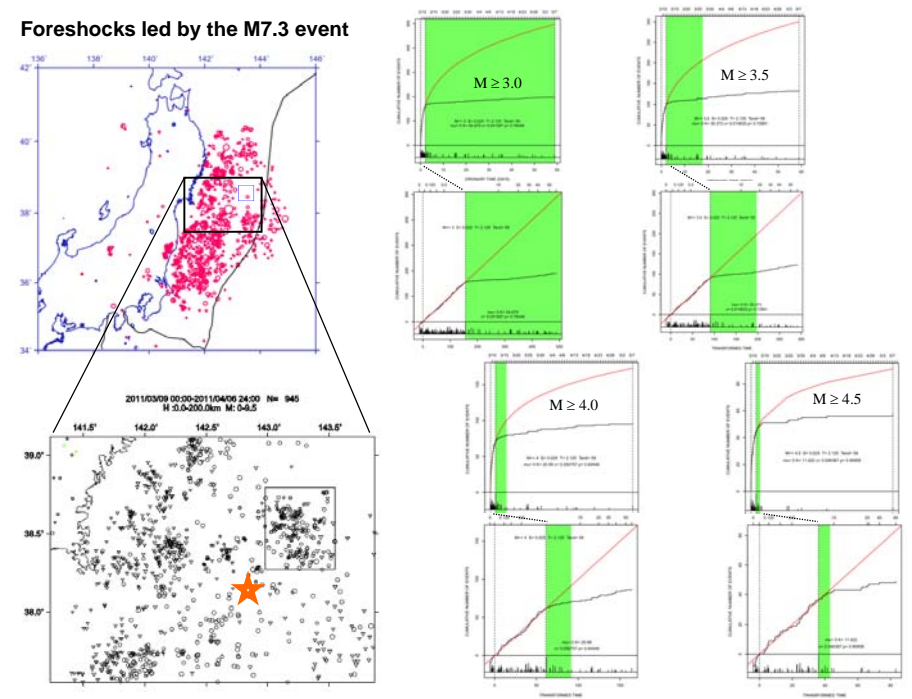
福島県いわき市付近の誘発地震活動



Foreshocks



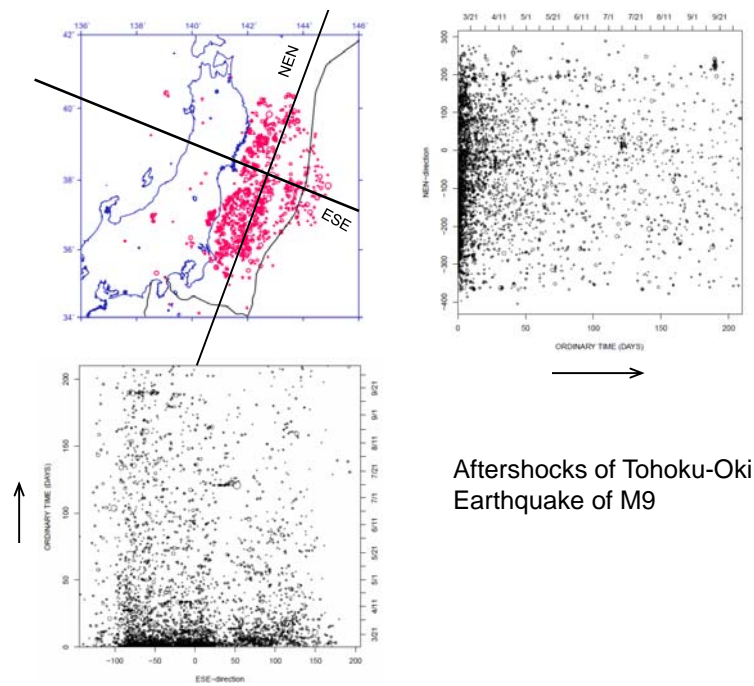
Foreshocks led by the M7.3 event



Space vs transformed-time plot of the foreshock activity till M9 mega event

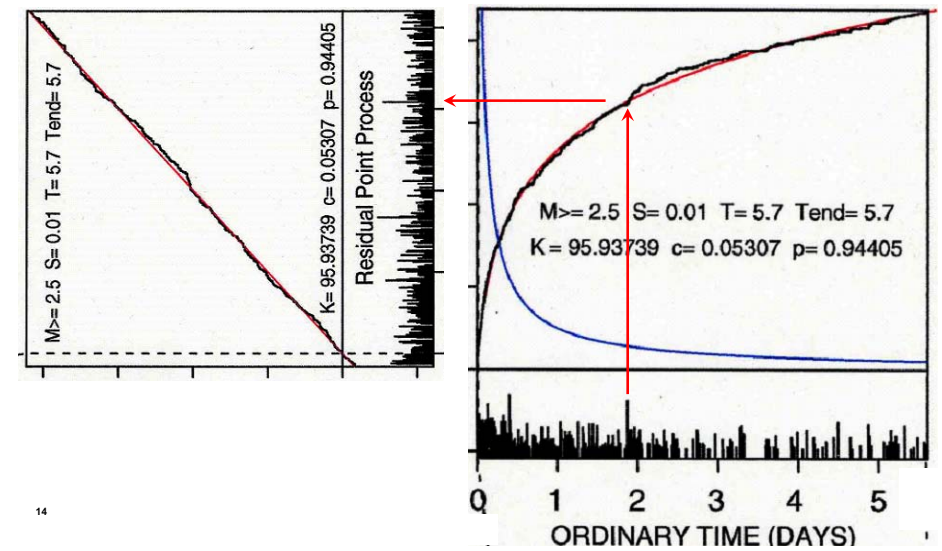
Aftershocks



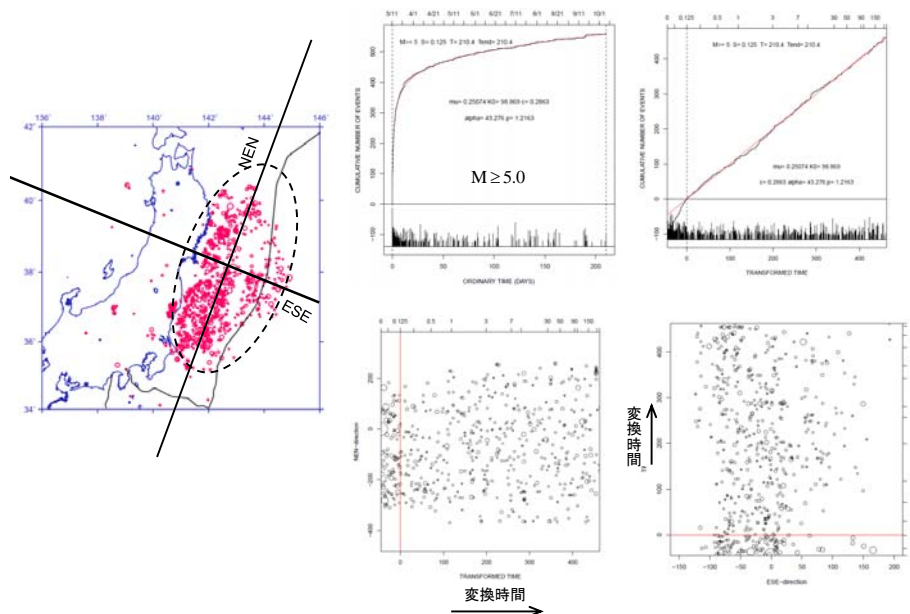


Theoretical cumulative number of the events:

$$\Lambda(t) = \int_0^t \lambda(s) ds$$

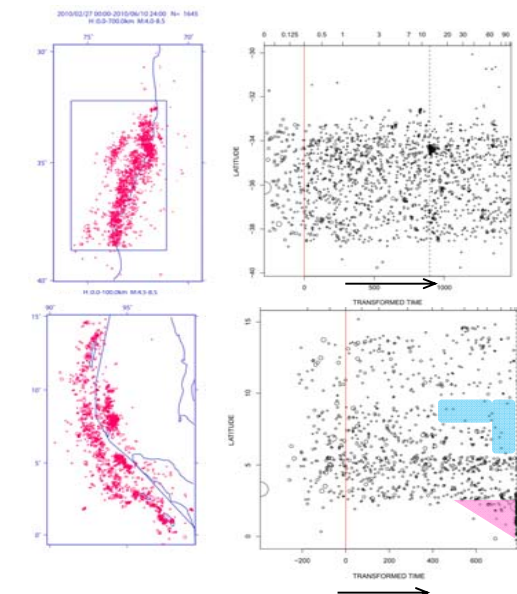


Aftershocks of Tohoku-Oki Earthquake of M9 (cont.)

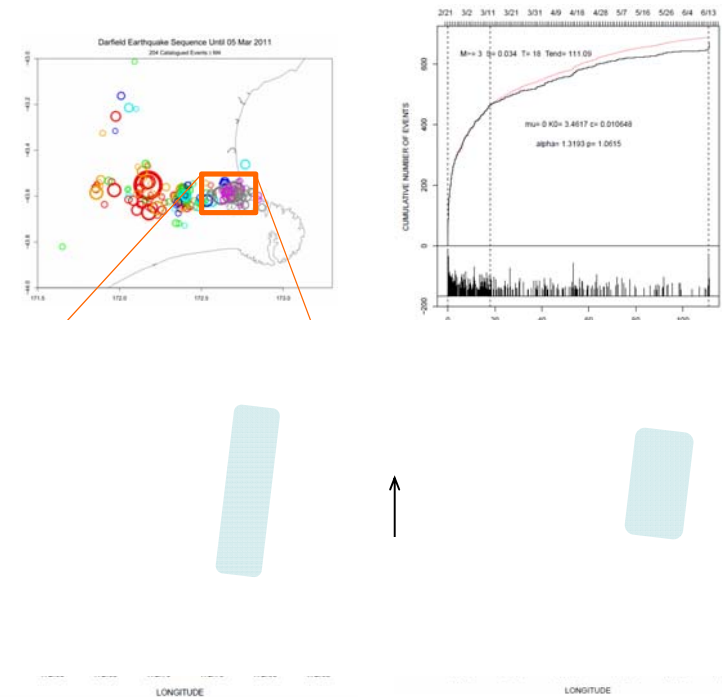
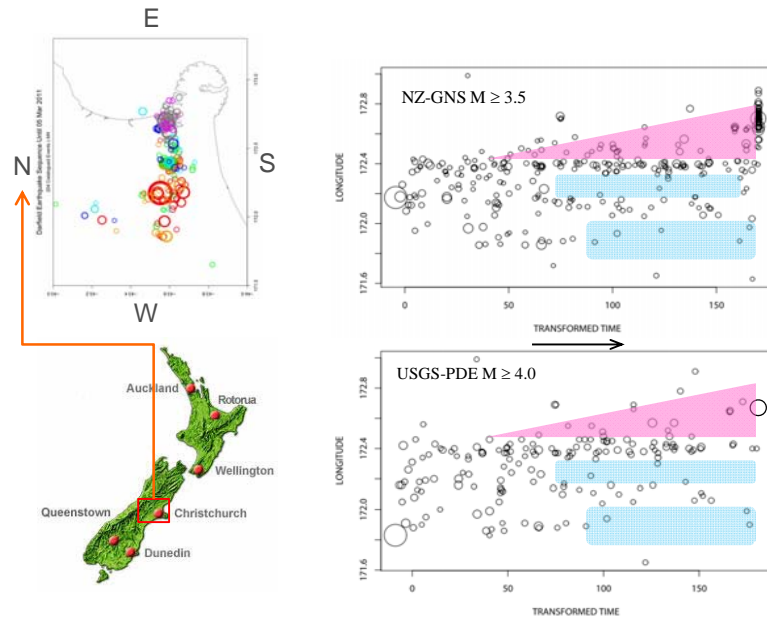


2010 Chili Earthquake (Mw8.8) Aftershocks

2004 Sumatra Earthquake (Mw9.0) Aftershocks



New Zealand Darfield Earthquake Aftershocks and Christchurch Earthquake



Extensive Quiescence before the M9 earthquake

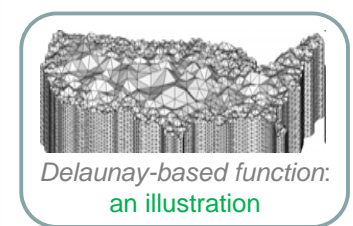
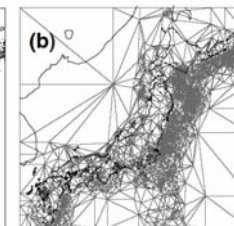
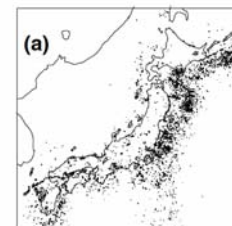


Space-Time ETAS model (Ogata, 1998, AISM)

$$\lambda(t, x, y) = \mu + \sum_{\{j: t_j < t\}} \frac{K}{(t - t_j + c)^p} \left\{ \frac{Q_j(x, y)}{e^{\alpha M_j}} + d \right\}^{-q}$$

Heterogeneity in Space (Ogata, 2004, JGR and 2011, EPS)

$$\begin{aligned} \mu &\Rightarrow \mu(x, y); \\ K &\Rightarrow K(x_j, y_j); \quad \alpha \Rightarrow \alpha(x_j, y_j); \\ p &\Rightarrow p(x_j, y_j); \quad q \Rightarrow q(x_j, y_j) \end{aligned}$$



Location Dependent Space-Time ETAS model
ETAS model and occurrence data
 $\{(t_i, x_i, y_i, M_i); i = 1, \dots, n\}$ in $[0, T] \times A$
 are given. Then **Log Likelihood** is

$$\log L(\theta) = \log L(\mu_{\theta_1}, K_{\theta_2}, \alpha_{\theta_4}, p_{\theta_5}, q_{\theta_7})$$

$$= \sum_{i=1}^n \log \lambda_{\theta}(t_i, x_i, y_i) - \int_0^T \int_A \lambda_{\theta}(t, x, y) dt dx dy.$$

where $\theta = (\theta_1, \theta_2, \theta_4, \theta_5, \theta_7)$

Penalized Log Likelihood

$$Q(\theta | w_{\mu}, w_K, w_{\alpha}, w_p, w_q)$$

$$= \log L(\theta) - \text{penalty}(w_{\mu}, w_K, w_{\alpha}, w_p, w_q)$$

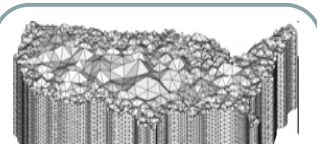
where the *penalty* is

$$\int \int_A dx dy \{w_1(\mu_x^2 + \mu_y^2) + w_2(K_x^2 + K_y^2) + w_3(\alpha_x^2 + \alpha_y^2) + w_4(p_x^2 + p_y^2) + w_5(q_x^2 + q_y^2)\}$$

Flatness constraints



Akaike Bayesian information criterion (Akaike, 1980)



*Delaunay-based function:
an illustration*

$$\rho = (w_{\mu}, w_K, w_{\alpha}, w_p, w_q)$$

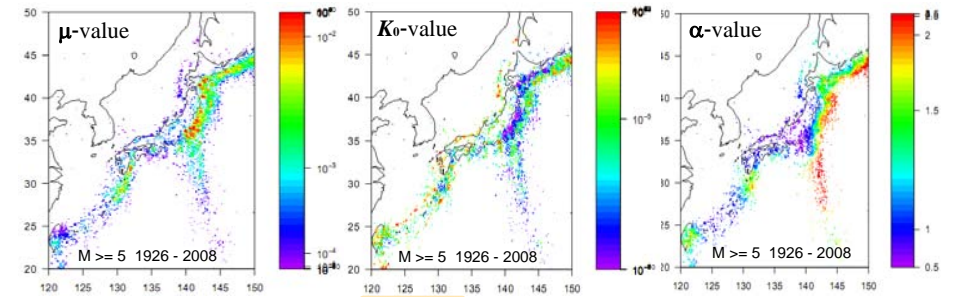
$$\text{posterior}(\theta | \rho) = \frac{L(\theta) \cdot \text{prior}(\theta | \rho)}{\Lambda(\rho)}$$

$$\Lambda(\rho) = \int \dots \int L(\theta) \cdot \text{prior}(\theta | \rho) d\theta$$

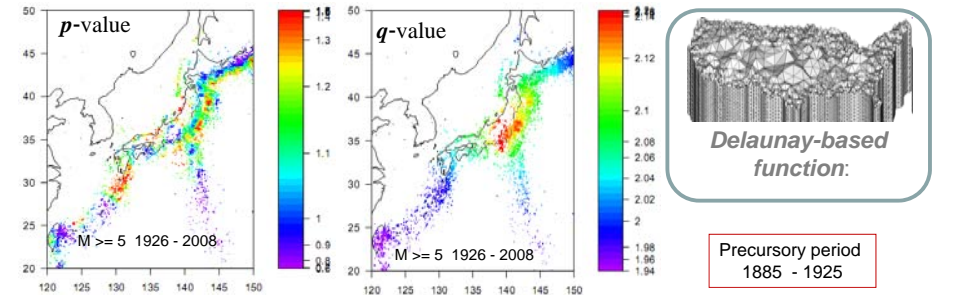
(Likelihood of a Bayesian model; Good 1965)

Choose ρ that maximize $\Lambda(\rho)$
 or minimize

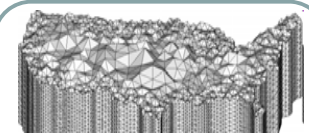
$$ABIC = (-2) \max_{\rho} \{\log \Lambda(\rho)\} + 2 \times \dim(\rho)$$



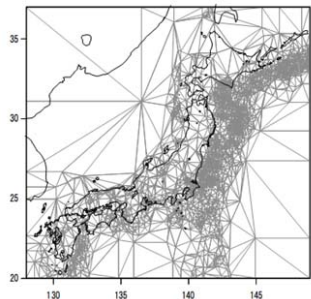
$$\lambda(t, x, y | H_t) = \mu(x, y) + \sum_{\{j: t_j < t\}} \frac{K_0(x_j, y_j)}{(t - t_j + c)^{p(x, y)}} \left[\frac{(x - x_j, y - y_j) S_j (x - x_j, y - y_j)^t}{e^{\alpha(x, y)(M_j - M_c)}} + d \right]^{-q(x, y)}$$



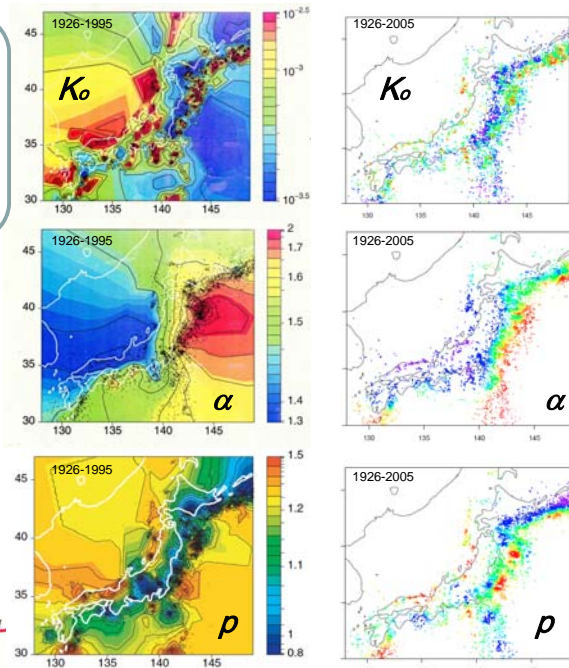
Precursory period
1885 - 1925



*Delaunay-based function:
an illustration*



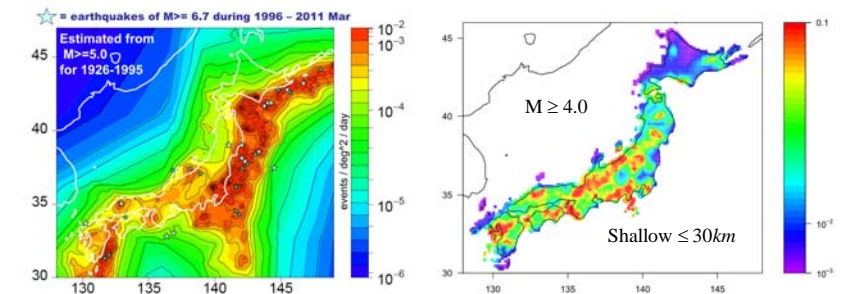
$$\lambda(t, x, y) = \mu + \sum_{\{j: t_j < t\}} \frac{K}{(t - t_j + c)^p} \left\{ \frac{Q_j(x, y)}{e^{\alpha M_j}} + d \right\}^{-q}$$



Hierarchical Space-time ETAS model (HIST-ETAS)

$$\lambda(t, x, y | H_t) = \mu(x, y) + \sum_{\{j: t_j < t\}} \frac{K(x, y)}{(t - t_j + c)^{p(x, y)}} \left[\frac{(x - x_j, y - y_j) S_j (x - x_j, y - y_j)^t}{e^{\alpha(x, y)(M_j - M_c)}} + d \right]^{-q(x, y)}$$

Background rate



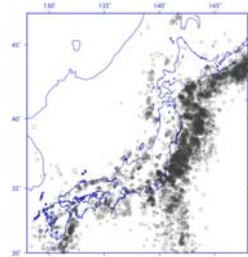
Stochastic declustering

(Zhuang, Ogata & Vere-Jones., 2004 JASA and 2005, JGR)

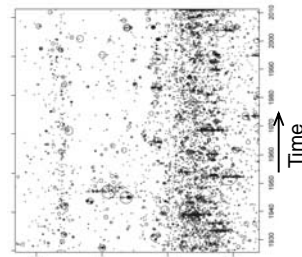
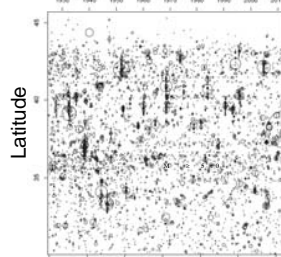
Accept earthquake i
 as a **background event** with probability:

$$\frac{\mu(x_i, y_i)}{\lambda(t_i, x_i, y_i | H_{t_i})}$$

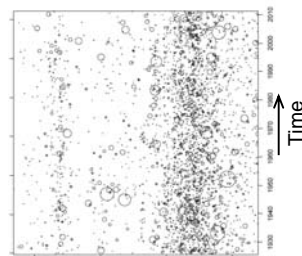
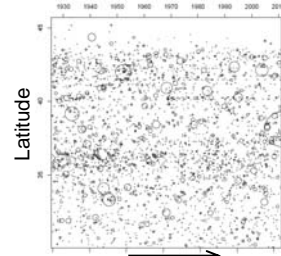
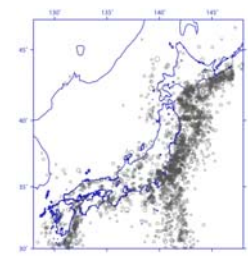
$M \geq 5.0$



Original data

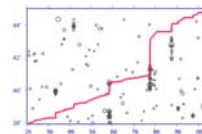


Time
De-clustered data

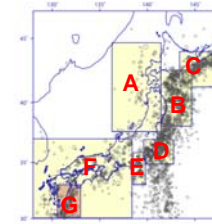


Longitude

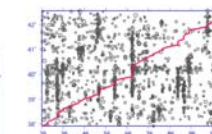
A



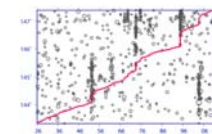
$M \geq 5.0$



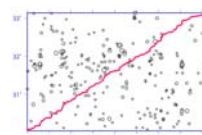
B



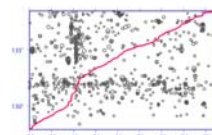
C



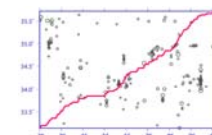
G



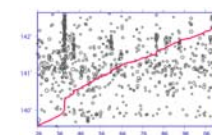
F



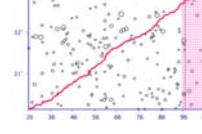
E



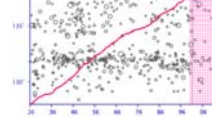
D



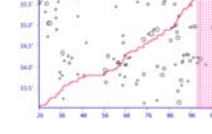
G



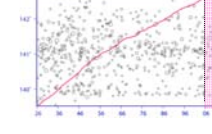
F



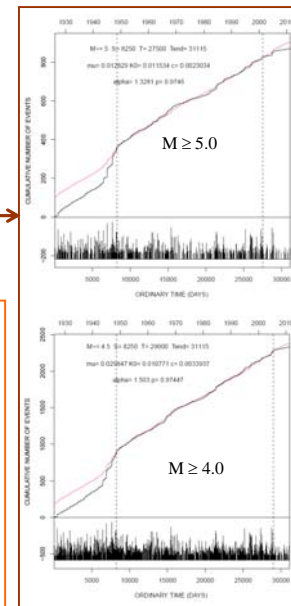
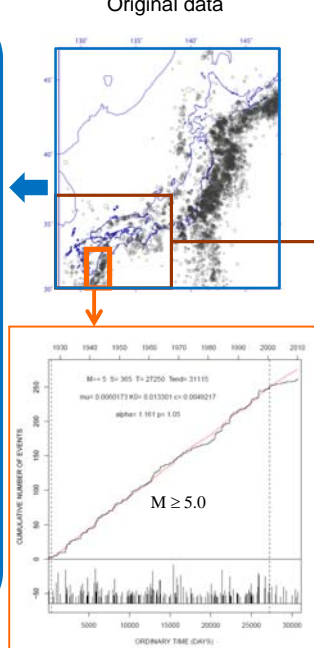
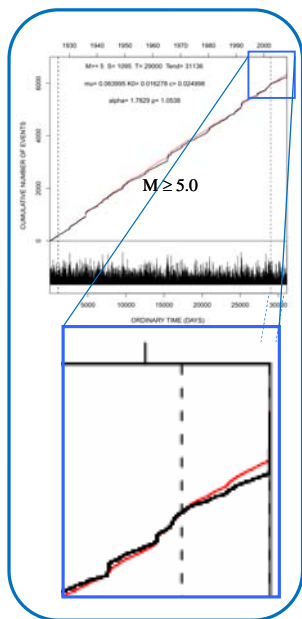
E



D

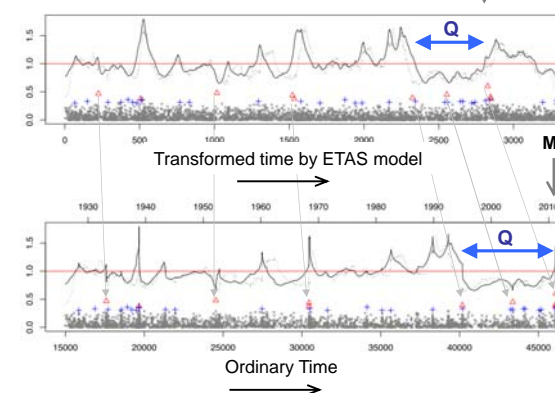
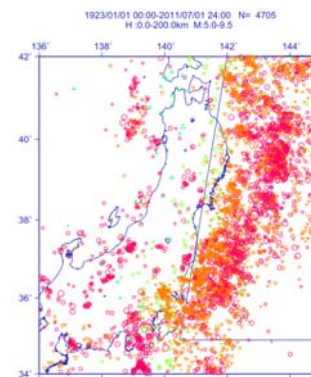


Original data

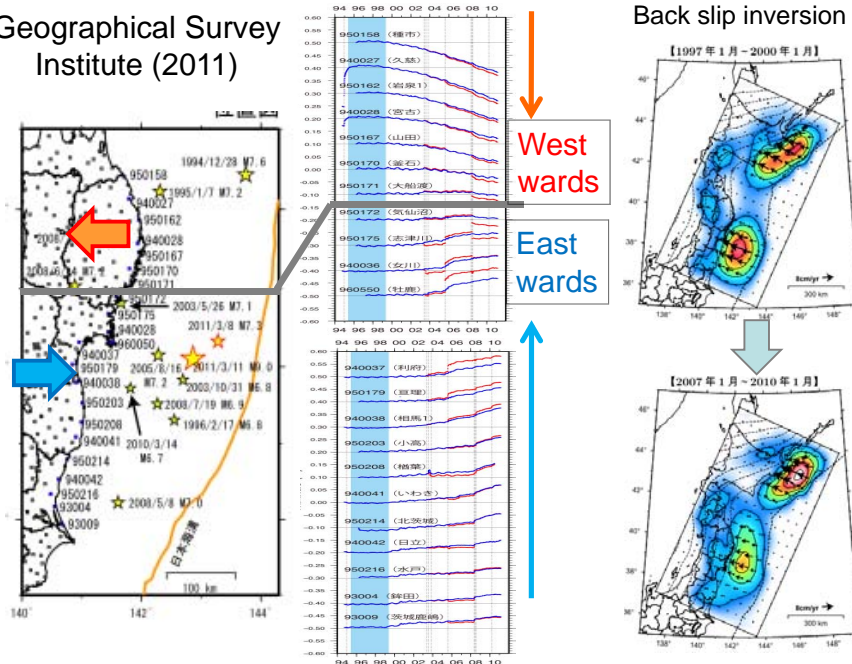


T. Kumazawa (SOKEN-DAI D3)

1926 ~ 2011 Mar. $M \geq 5.0$



Geographical Survey Institute (2011)

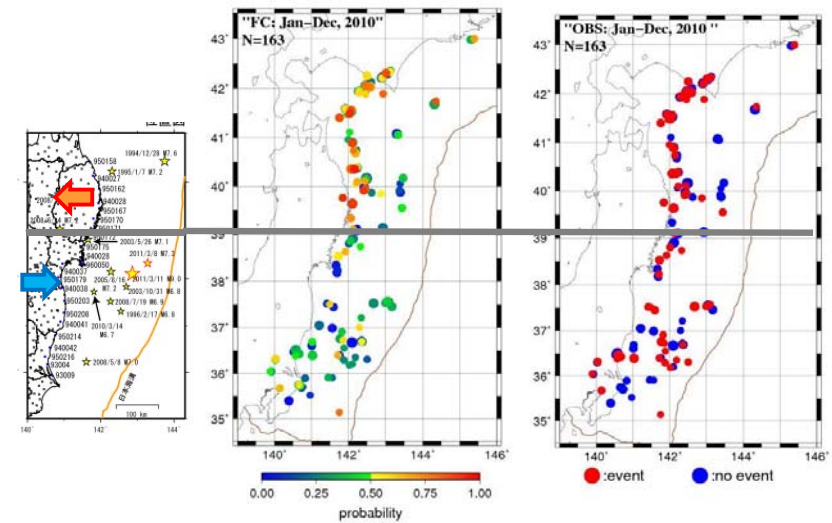


Okada, Uchida, Aoki (2011)

Renewal model (log Normal) for 163 repeating earthquake sequences
Estimation 1993 - 2009

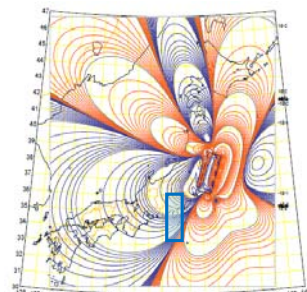
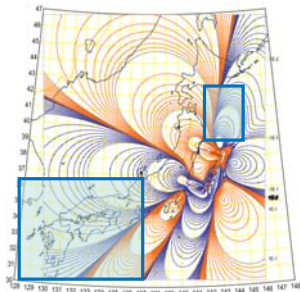
Forecasted for 2010

Result for 2010



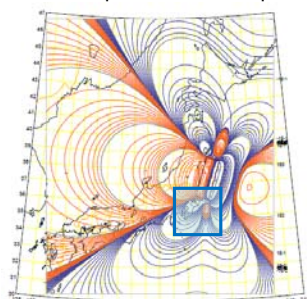
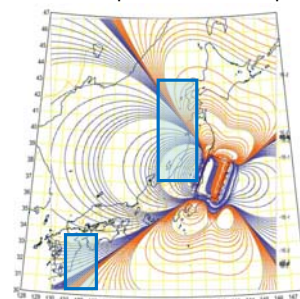
E-W compression strike slips

N-S compression thrust slips



E-W compression thrust slips

N-S compression strike slips



**Operational Probability
Forecasting of Foreshocks
and Evaluations:**
15 years periods till the Tohoku-Oki Event



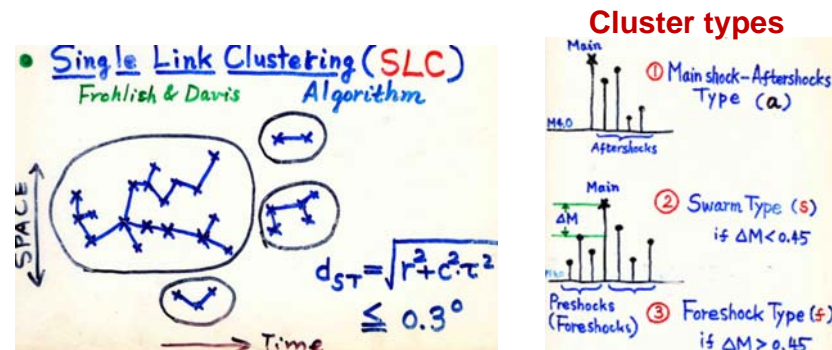
(1) How do we recognize that it is initial earthquake of a cluster?

(2) What is definition of foreshocks?

Earthquakes ($M \geq 4.0$) in JMA catalog during 1994 ~ Mar. 2011 are connected by the distance criterion

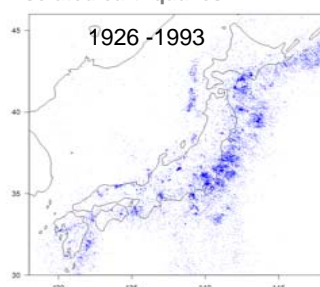
$$d_{ST} = \sqrt{\Delta_{space}^2 + (c\Delta_{time})^2} \leq 0.3^\circ \text{ (or 33.33km)}$$

where c is the constant so as to hold 1day = 1km

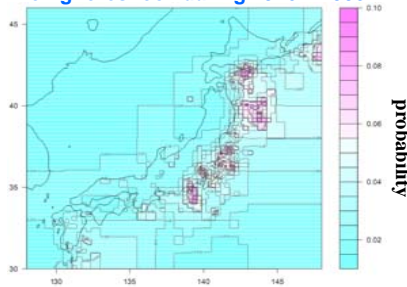


Single-link-clustering 1926-1993, $M \geq 4$ from the old JMA catalog								
Cluster member#	Foreshocks			Swarms			M.A.	All clusters
	#c	ratio(%)	s.e.(%)	#c	ratio(%)	s.e.(%)	#c	#c
≥ 1	467	3.7	± 0.2	--	--	--	11676	12727
≥ 2	125	6.5	± 0.6	584	30.5	± 1.1	1207	1916
≥ 3	57	8.0	± 1	271	37.9	± 1.8	387	715
≥ 4	33	8.7	± 1.5	153	40.5	± 2.5	192	378
≥ 5	18	7.4	± 1.7	93	38.4	± 3.1	131	242
≥ 6	12	6.8	± 1.9	63	35.6	± 3.6	102	177
≥ 7	10	7.9	± 2.4	44	34.6	± 4.2	73	127
≥ 8	8	7.8	± 2.6	31	30.1	± 4.5	64	103
≥ 9	8	9.2	± 3.1	29	33.3	± 5.1	50	87
≥ 10	8	10.3	± 3.4	25	32.1	± 5.3	45	78

Initial earthquakes of clusters or isolated earthquakes



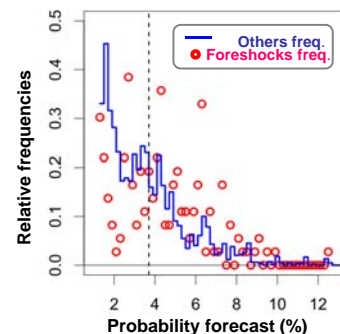
Probability of the initial earthquakes Being foreshock during 1926 - 1993



Forecasted results for 1994 - Mar

Forecast	0-2.5%	2.5-5%	5%-	All
Foreshocks	33	84	65	182
Others	1572	1849	770	4191
All types	1605	1933	835	4373
Ratio (%)	2.1	4.3	7.8	4.2

Diff. entropy = -22.7
Diff. AIC = -40.0 (cross-table)



Measuring inter-events concentrations in a cluster and magnitude increments

$(t_i^c, x_i^c, y_i^c, M_i^c)$:
Hypocenters in a cluster $c \in C$

① Origin-time differences

$$t_{ij}^c = t_j^c - t_i^c$$

for any pairs i, j such that $i < j$

② Epicenter separations

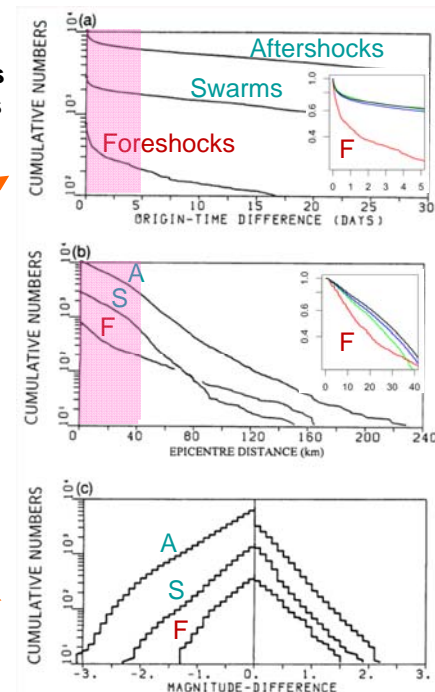
$$r_{ij}^c = \sqrt{(x_j^c - x_i^c)^2 + (y_j^c - y_i^c)^2}$$

($i < j$)

③ Magnitude differences

$$M_{ij}^c = M_j^c - M_i^c$$

($i < j$)



Time difference, Distance & Magnitude difference Normalization

$$(t, r, g) \rightarrow (\tau, \rho, \gamma) \text{ in } [0,1]^3 \quad \equiv$$

Time Interval Transformation

$$\tau = \begin{cases} 0 & \text{for } t \leq 0.01 \\ \log(100t) / \log(3000) & \text{for } 0.01 < t \leq 30 \\ 1 & \text{for } 30 \leq t \end{cases}$$

Epicenter Separation Transformation

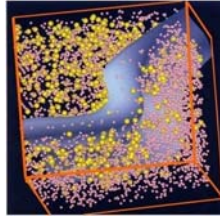
$$\rho = 1 - \exp\{-\min(r, 50) / 20\}$$

Magnitude Difference Transformation

$$\gamma = \begin{cases} (2/3) \exp\{g/\sigma_1\} & \text{for } g \leq 0 \\ (2/3) + (1/3)[1 - \exp\{-g/\sigma_2\}] & \text{for } g > 0 \end{cases}$$

ただし $\sigma_1 = 6709, \sigma_2 = 0.4456$

Normalized time difference,
distance & magnitude
difference in the unit cube



Algorithm of foreshock probability calculations in case of plural earthquakes in a cluster

For plural earthquakes in a cluster, time differences t_{ij} (days), epicenter separation r_{ij} (km), magnitude difference g_{ij} are transformed into the unit cube

$$(t_{i,j}, r_{i,j}, g_{i,j}) \rightarrow (\tau_{i,j}, \rho_{i,j}, \gamma_{i,j}) \in [0,1]^3$$

Probability p_c is calculated sequentially

$$\text{logit}(p_c) = \text{logit}\{\mu(x_1, y_1)\} + \frac{1}{\#\{i < j\}} \sum_{i < j} \left[a_1 + \sum_{k=1}^3 b_k \gamma_{i,j}^k + \sum_{k=1}^3 c_k \rho_{i,j}^k + \sum_{k=1}^3 d_k \tau_{i,j}^k \right]$$

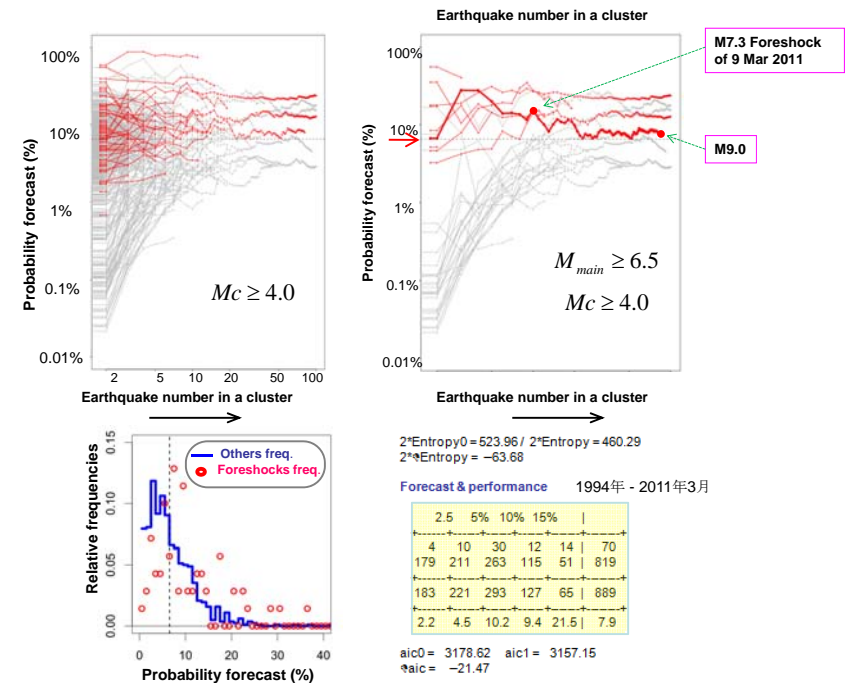
Here $\mu(x, y)$ indicates probability of initial earthquake at location (x, y) , and the 2nd term calculates arithmetic mean of polynomials of the normalised space-time magnitude variables for all pairs of earthquakes $(i < j)$ in a cluster, where the coefficients a, b, c, d are as follows.

Ogata, Utsu and Katsura, 1996, GJI				
k	a_k	b_k	c_k	d_k
1	8.018	-33.25	-1.490	-10.92
2		62.77	2.805	295.09
3		-37.66	-2.190	-1161.5

Forecasted sequence and evaluation (1994–2011Mar)

# F?	#C	Pc	ENTRYP	CU-ENT	P1	P2	P3	P4	P5	P6	P7	P8	P9	P10
1	-	1	5.14%	-0.01537	-0.01537	5.14%								
2	-	2	10.06%	-0.06863	-0.08400	7.46%	12.66%							
3	-	1	18.58%	-0.16822	-0.25222	18.58%								
4	-	1	10.71%	-0.07592	-0.32814	10.71%								
5	-	1	0.15%	0.03586	-0.29228	0.15%								
6	-	1	1.70%	0.02028	-0.27200	1.70%								
7	-	4	9.50%	-0.06243	-0.33443	9.14%	11.17%	7.87%	9.82%					
8	-	1	6.03%	-0.02484	-0.35927	6.03%								
9	-	1	1.77%	0.01950	-0.33977	1.77%								
10	+	1	13.14%	1.27605	0.93628	13.14%								
.....														
875	+	80	9.2%	0.923	28.649	6.7%	27.8%	27.7%	20.1%	14.0%	14.2%	13.6%	11.6%	15.7%
						10.1%	8.2%	10.1%	11.7%	10.9%	10.6%	11.5%	11.1%	9.9%
						7.2%	6.8%	7.6%	7.3%	7.4%	6.7%	7.0%	7.0%	8.0%
						8.6%	8.2%	8.0%	8.1%	8.4%	7.8%	7.3%	7.5%	7.8%
						8.1%	7.8%	7.4%	7.7%	7.8%	7.6%	7.2%	7.2%	6.9%
						6.7%	7.4%	8.0%	7.8%	7.6%	7.7%	8.3%	9.0%	8.7%
						8.6%	8.3%	8.4%	8.2%	8.2%	8.0%	7.9%	7.9%	8.4%
						8.6%	8.5%	8.6%	8.4%	8.2%	8.4%	8.3%	8.3%	8.1%
														7.9%
.....														
880	-	11	2.44%	0.01266	31.60644	4.69%	4.77%	6.21%	3.42%	1.74%	1.24%	1.04%	0.90%	0.83%
						1.03%								0.97%
881	-	16	2.11%	0.01604	31.62248	0.03%	0.25%	0.51%	0.83%	2.77%	2.21%	2.02%	3.19%	2.78%
						2.43%	3.07%	2.92%	2.74%	2.84%	2.68%			2.50%
882	-	7	1.47%	0.02259	31.64507	0.06%	0.79%	1.70%	2.06%	1.90%	1.90%	1.88%		
883	-	1	4.51%	-0.00878	31.63629	4.51%								
884	-	1	3.84%	-0.00178	31.63451	3.84%								
885	+	7	5.04%	0.31698	31.95149	6.89%	7.42%	4.88%	3.98%	3.56%	4.05%	4.49%		
886	-	1	2.84%	0.00853	31.96002	2.84%								
887	-	1	7.00%	-0.03518	31.92483	7.00%								
888	-	1	7.65%	-0.04219	31.88264	7.65%								
889	-	1	7.83%	-0.04419	31.83845	7.83%								

2*Entropy0 = 523.96; 2*Entropy = 460.29; 2*Entropy = -63.68



Thank you very much
for your attention.

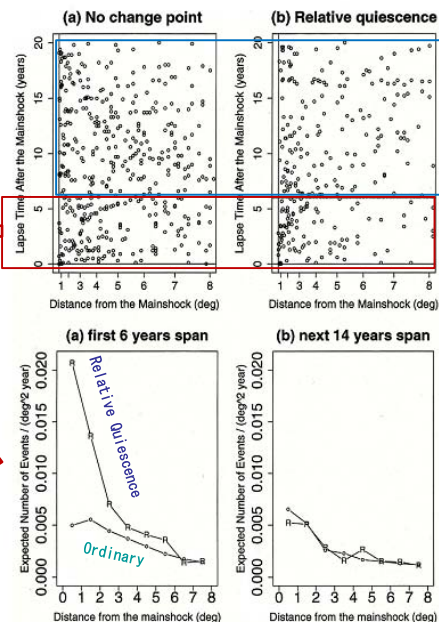
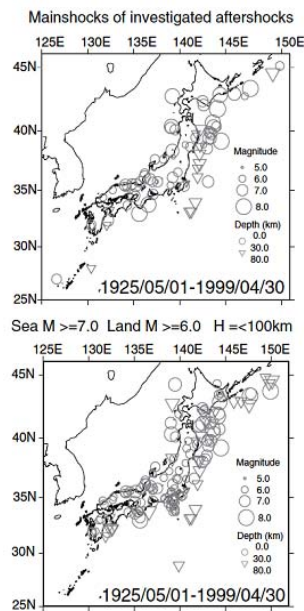
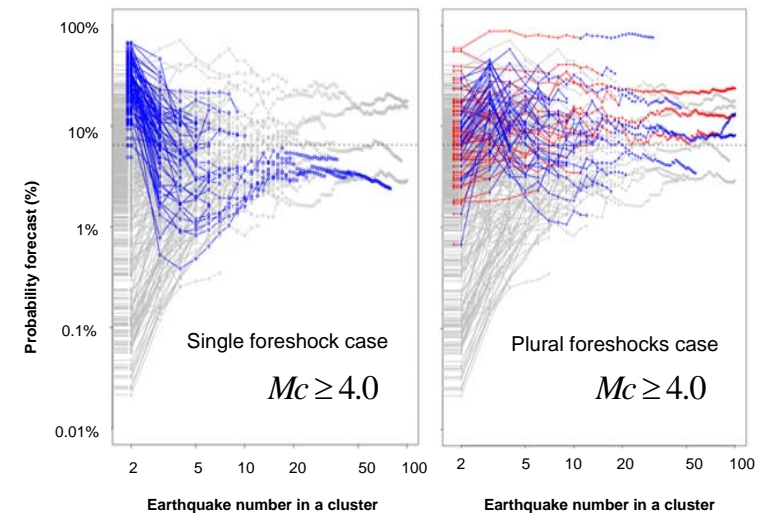
Software available for the ETAS fitting,
diagnostic analysis and its manual. Please
visit WEB home page of our project team:

<http://www.ism.ac.jp/~ogata/Ssg/ssgE.html>

Very soon, computer programs
are available for the Hierarchical
Space-Time ETAS (HIST-ETAS)
by a Bayesian procedure (ABIC).



How foreshock forecast probabilities (BLUE LINES) changed after
actual mainshock occurred in case of foreshock-mainshock-
aftershock sequence?

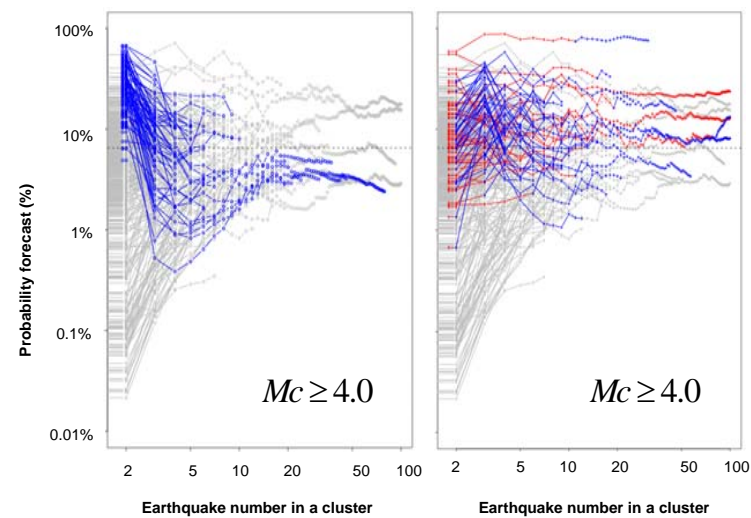


Single-link-clustering 1926-1993, $M \geq 4$ from the old JMA catalog						
Cluster member#	#c	ratio(%)	s.e.(%)	#c	ratio(%)	s.e.(%)
1	467	3.7 ± 0.2	—	—	11676	12727
2	125	6.5 ± 0.6	584	30.5 ± 1.1	1207	1916
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10	8	10.3 ± 3.4	25	32.1 ± 5.3	45	78

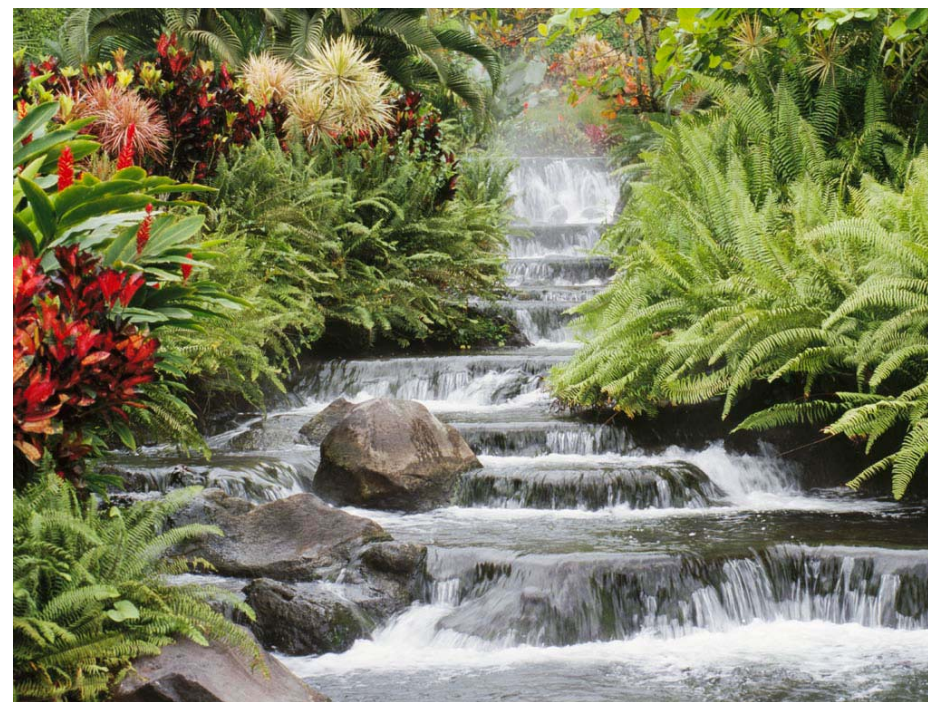
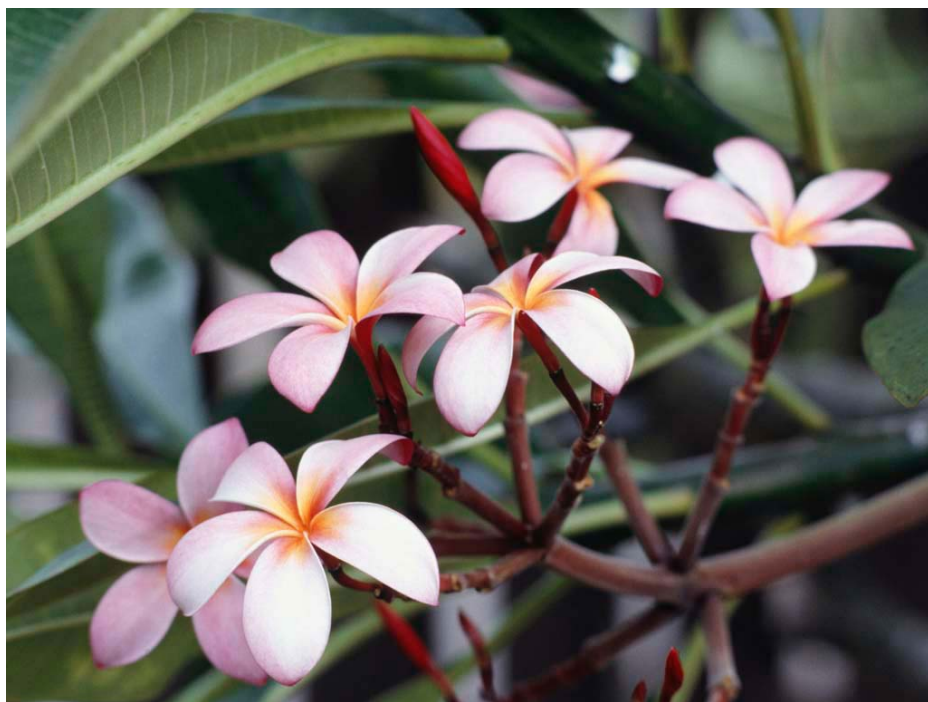
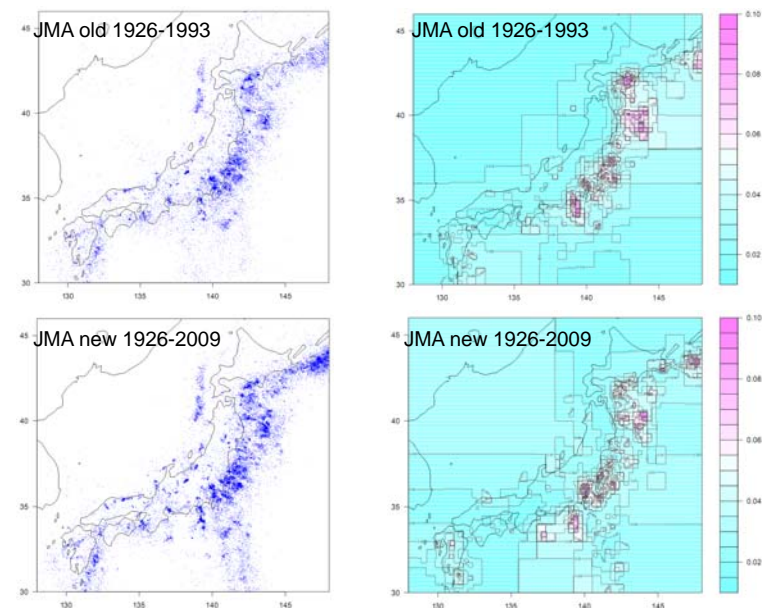
Single-link-clustering 1926-2009, $M \geq 4$ from the new JMA catalog						
Cluster member#	#c	ratio(%)	s.e.(%)	#c	ratio(%)	s.e.(%)
1	1088	6.5 ± 0.2	—	—	14872	16784
2	156	5.6 ± 0.4	824	29.6 ± 0.9	1800	2780
3	78	7.6 ± 0.8	366	35.4 ± 1.5	589	1033
4	46	8.2 ± 1.2	213	38.2 ± 2.1	299	558
5	30	7.9 ± 1.4	145	38.1 ± 2.5	206	381
6	20	7.1 ± 1.5	108	38.2 ± 2.9	155	283
7	15	7.0 ± 1.7	77	36.0 ± 3.3	122	214
8	13	7.6 ± 2	59	34.7 ± 3.7	98	170
9	11	7.9 ± 2.3	46	33.1 ± 4	82	139
10	11	8.7 ± 2.5	44	34.9 ± 4.2	71	126

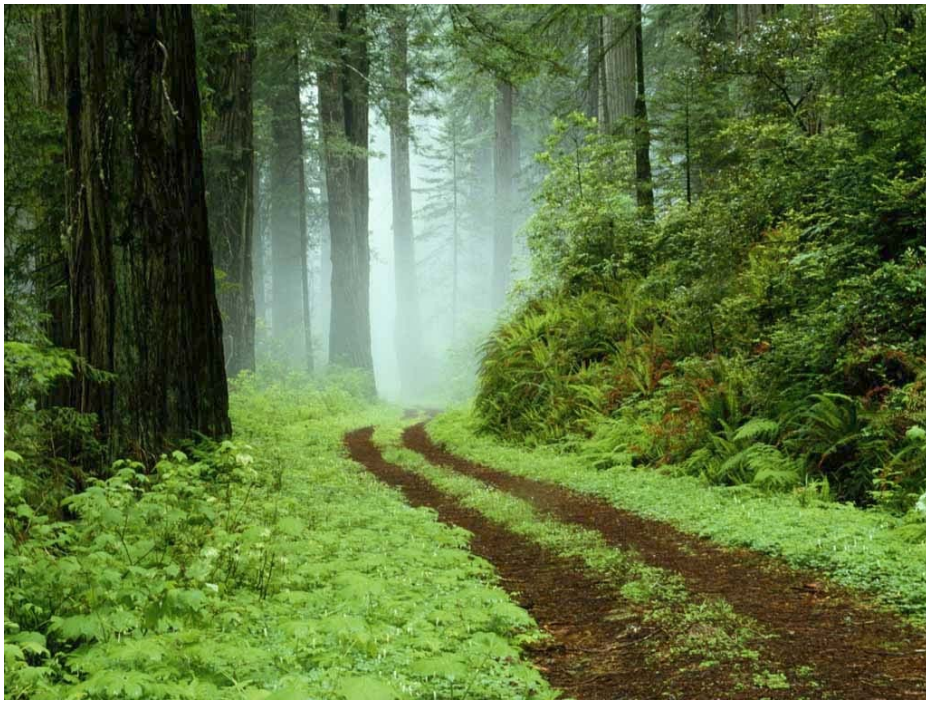
前震の確率は本震が起きてからどのように変わったか？

・青線が本震直前以降の確率変化。左図が一個の前震の場合で右図が複数の前震(赤線)の場合。



群れの先頭(孤立地震を含む)が前震である確率の地域性





Thank you very much for your attention



Software available.
Please visit WEB home page of our project team:
<http://www.ism.ac.jp/~ogata/Ssg/ssgE.html>